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Noise-based techniques for gas sensing

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Outline

- Introduction to noise and fluctuation-enhanced sensing (FES)
- Adsorption-desorption noise in gas sensors
 - Frequency and time domain response
- $1/f$ noise in gas sensors
- Higher order statistics
- Precautions
- Conclusions

Introduction-general

- **Electronic nose:**
 - arrays of N detectors with different selectivity for detection of M species ($N \gg M$)
 - Pattern recognition algorithms for selectivity
- **Noise** is considered as detrimental in sensing as it reduces the S/N ratio
- But noise is also a **signal** [Bruschi & *Sensors and Actuators B*, **19** (1994) 421]
- **Fluctuation enhanced sensing (FES):** [Kish & *Sensors and Actuators B*, **71** (2000) 55]
 - employ patterns in noise characteristics of microfluctuations (e.g. spectra)
 - → **reduction** of number of sensing elements
 - **In theory:** one sensor could resolve mixture of gases

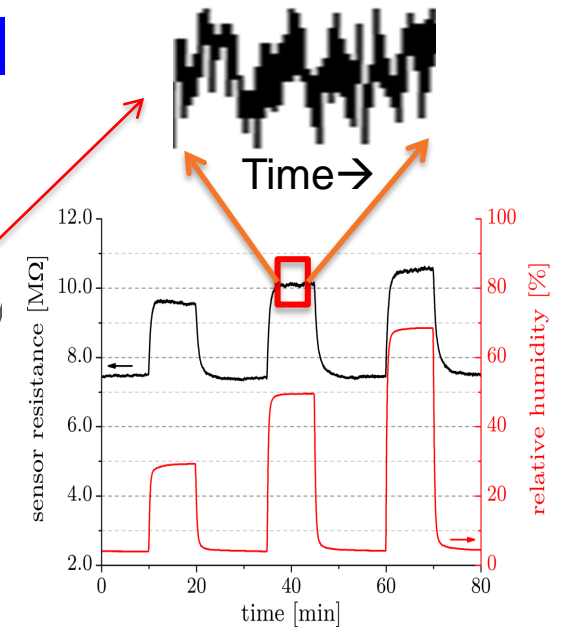


fig. from [Steinhauer et al. APL2014]

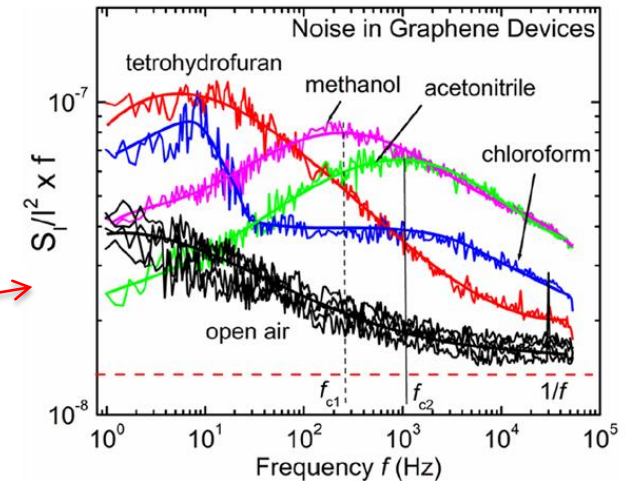


fig from [Rumyantsev, Nanolett. 12 (2012) 2294]

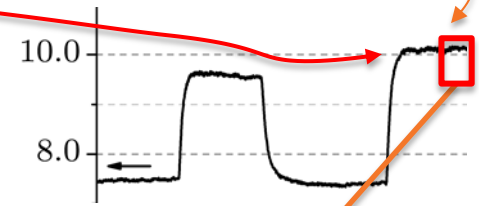
Noise basics

- We are interested in **stationary** fluctuations!!!: $I(t)$, $U(t)$, $R(t)$, $G(t)$...

Mean value

$$I_{TOTAL}(t) = \langle I \rangle + I(t)$$

Stochastic component

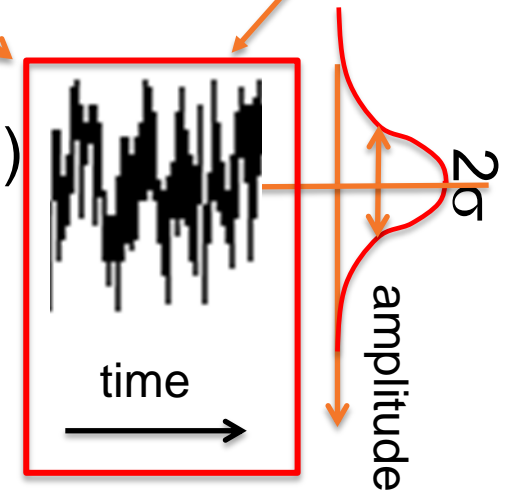


$$I(t) \xrightarrow{\text{FFT}} Y(\omega) = \int I(t) \exp(-i\omega t) dt$$

$$S_I(\omega) = \lim_{T \rightarrow \infty} \int \frac{2|Y(\omega)|^2 d\omega}{T}$$

Power spectral density (PSD) of current fluctuations

$$\sigma^2 = \text{var} = \langle (I(t) - I_{mean})^2 \rangle = \int S_I(f) df$$



PSD is FFT of autocorrelation function $c(\tau) = \langle I(t)I(t + \tau) \rangle$

$$S_I(\omega) = 4 \int c(\tau) \cos(\omega\tau) d\tau \rightarrow \text{different time domain waveforms can give the same PSD} \rightarrow \text{information lost}$$

Noise in (chemi-)resistors

$$I(t) \approx qN(t)\mu(t)E$$

$$S_I(\omega) \propto (dI)^2$$

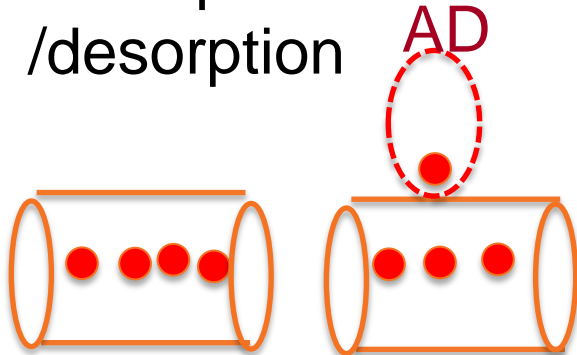
$$dI \approx \mu dN + Nd\mu$$

$$\frac{S_I}{I^2} = \frac{S_U}{U^2} = \frac{S_R}{R^2} = \frac{S_G}{G^2}$$

Carrier number fluctuations

Mobility fluctuations

Adsorption
/desorption

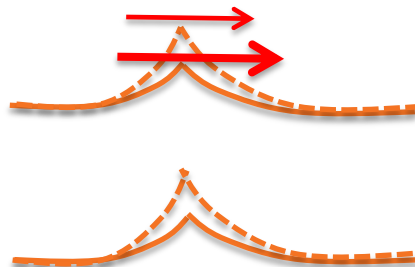


N ↔ N-dN

[Gomri&, J.Phys. D.Appl. Phys41(2008)065501]

RATION IN

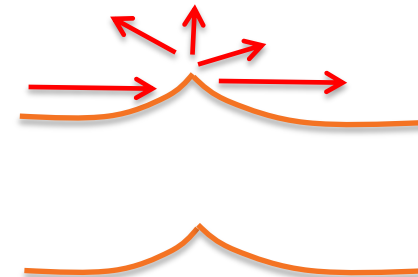
Barrier height
fluctuations at
grain boundaries



Surface diffusion too

[Schmera&, I3E Sens J.10(2010)461]

Scattering on defects
(charged, surface
roughness,...)

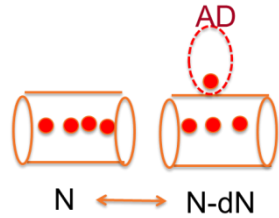


[Hooge, I3E TED, 41(1994)1926]

Adsorption / desorption (A/D) noise

[In semiconductors known as generation-recombination and random telegraph signal (RTS) noise (defect occupancy fluctuations)]

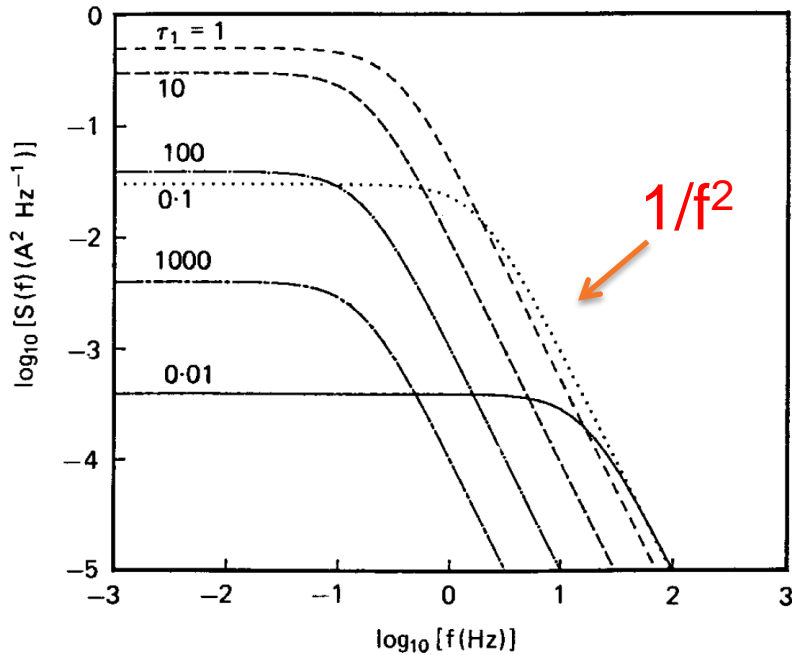
$$dN=1$$



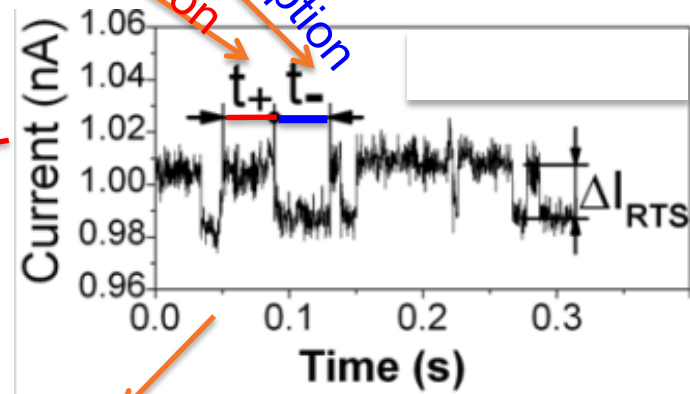
$$\tau = \frac{1}{(1/\tau_{ad} + 1/\tau_{des})} \quad S_I(f) = \frac{\tau^2}{(\tau_{ad} + \tau_{des})} \frac{4(\Delta I)^2}{1 + [2\pi f \tau]^2}$$

[Machlup, JAP, 25(1954)341]

Lorentzian



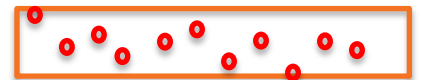
spectrum



Single A/D events (one site)

$$\tau_{ad} = t_+ \\ \tau_{des} = t_-$$

Ensemble of sites with the same A/D time constant



Ensemble averaging

spectrum



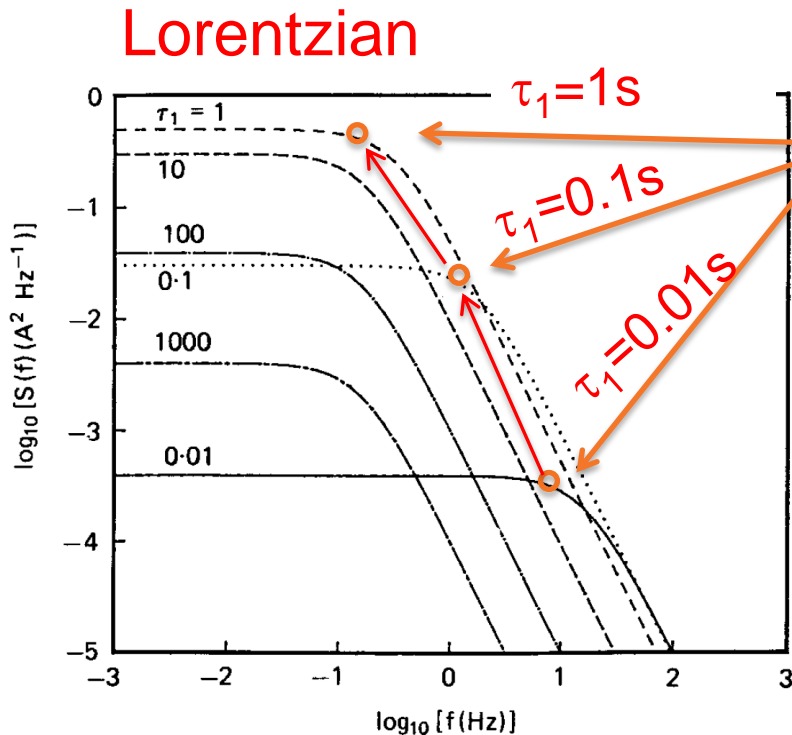
Lorentzian power spectra calculated using equation (2.19 a). $\Delta I = 1 \text{ A}$, $\tau_0 = 10 \text{ s}$, $\tau_1 = 0.01-1000 \text{ s}$.

Adsorption / desorption (A/D) noise

Number of active sites

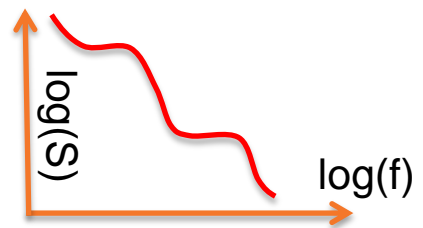
$$S_I(f) \propto \frac{\tau^2}{(\tau_{ad} + \tau_{des})} \frac{N_{sites}}{1 + [2\pi f \tau]^2}$$

$$\tau = \frac{1}{(1/\tau_{ad} + 1/\tau_{des})}$$



Spectral features:

- corner frequency: $f_{cor} = 1/(2\pi\tau)$
- \rightarrow multiple Lorentzians in a mixture of gases

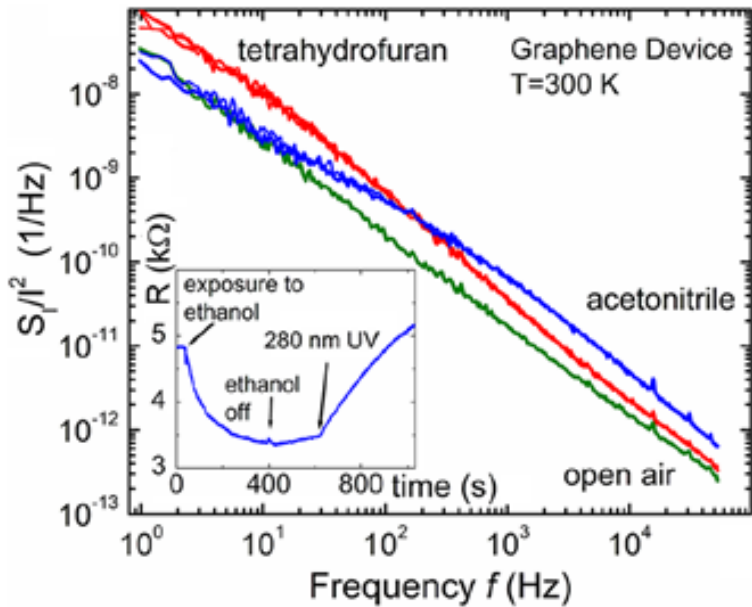


- $\tau_{ad} = f_{ad}(T, p_i, \dots)$ $\tau_{des} = f_{des}(T, p_i, \dots)$
- f_{cor} depends on temperature T and partial pressures p_i
- maximum amplitude of PSD occurs for $\tau_{ad} = \tau_{des} \rightarrow$ proper choice of T, p_i

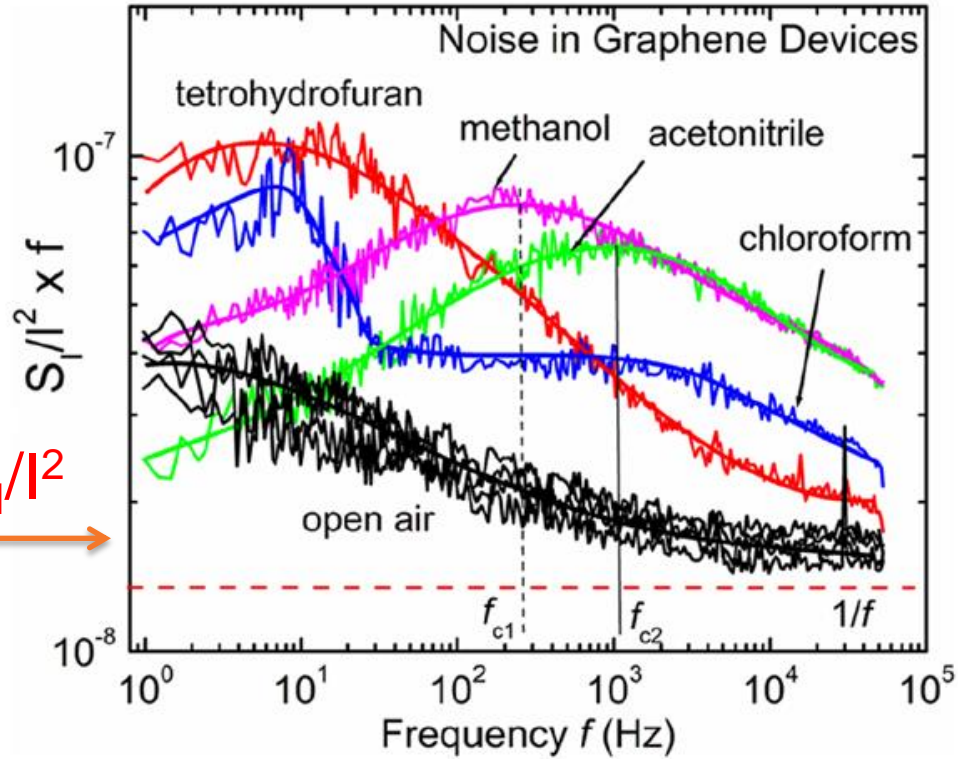
Fig from [Kirton&Uren, Adv. Phys.1989]

Graphene sensor

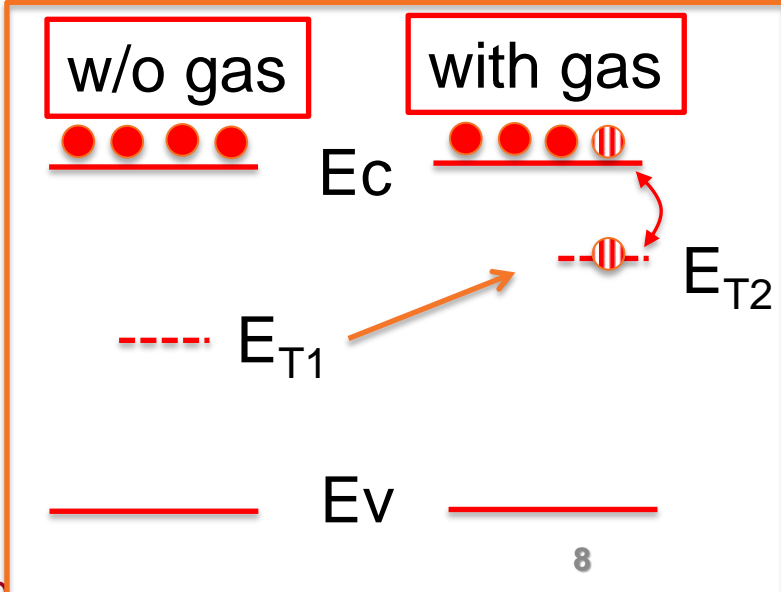
Lorentzian superimposed on $1/f$



$f \cdot S_I^2$



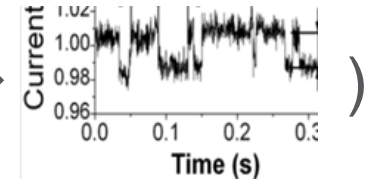
- Reproducible f_{cor} for different gases
 - but the A/D time constants from the $R(t)$ measurements are much higher (\approx min) than that corresponding to f_{cor} (1-100 ms)
 - gas covering can induce g-r noise (modification of existing surface states)
- [Rumyantsev, Nanolett. 12 (2012) 2294]



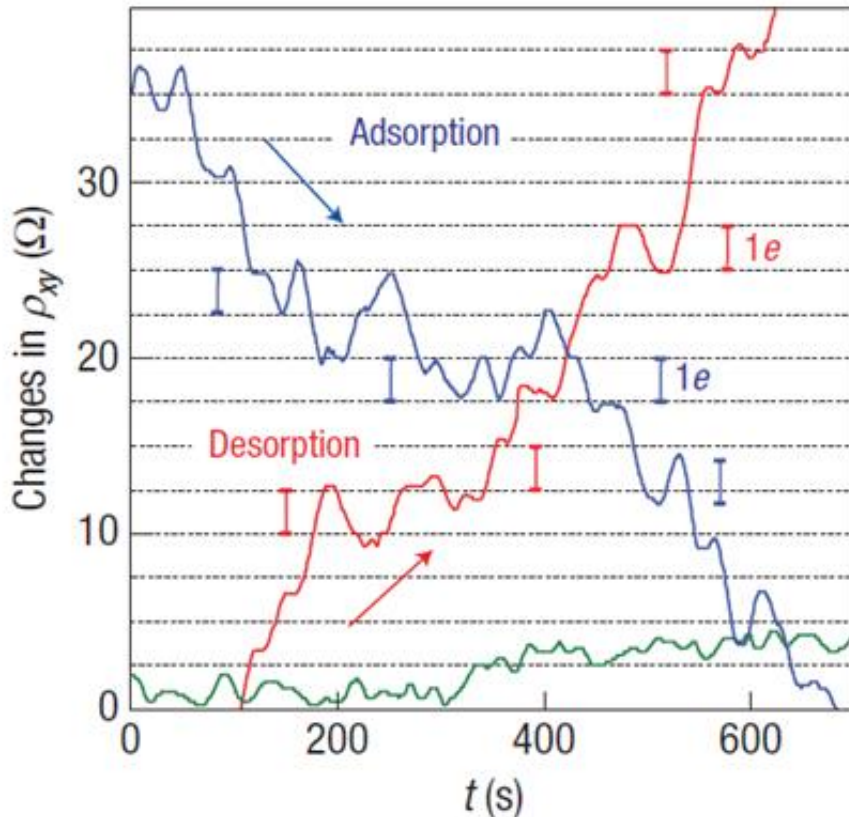
MoS₂,...tooooo

Single adsorption/desorption events in graphene

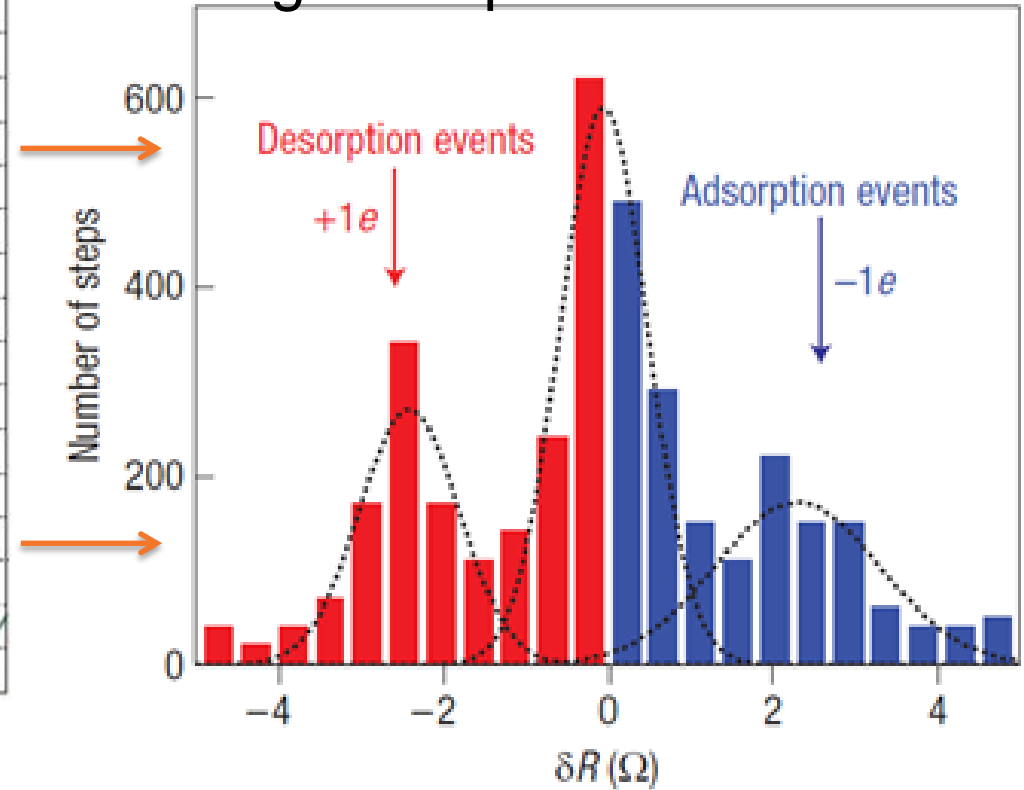
- Exposure to low concentration of NO₂
- Non-equilibrium situation (if equilibrium \rightarrow RTS \rightarrow)



Discrete steps: A/D of individual molecules



Histogram of resistance steps during desorption of NO₂



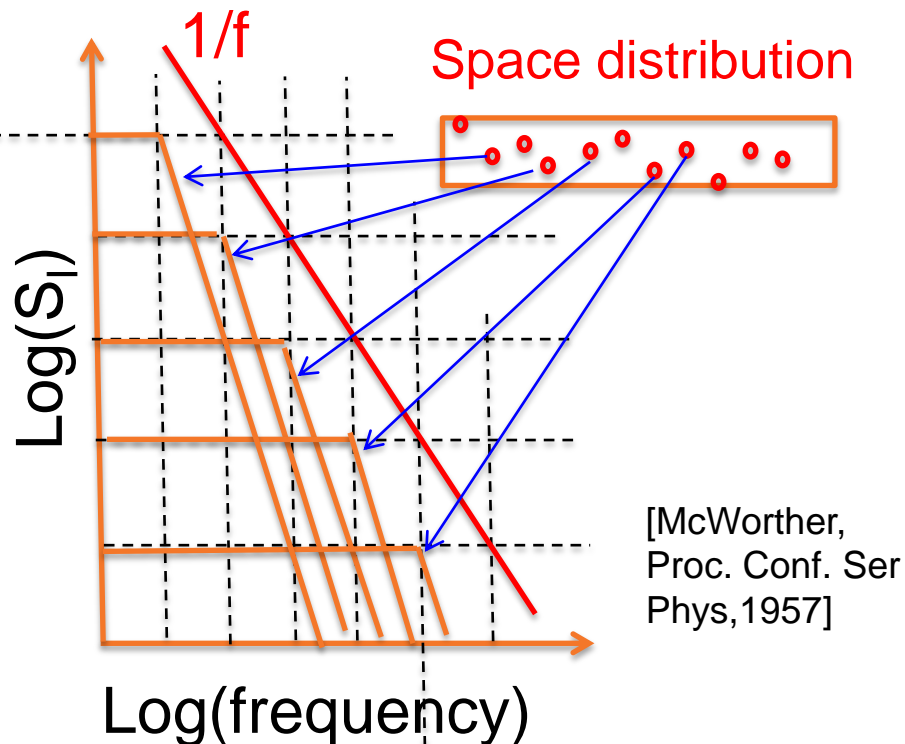
from [Shedin&, Nature, 6(2007)652]

LOGY

Quantized change in $R(t) \rightarrow$ A/D

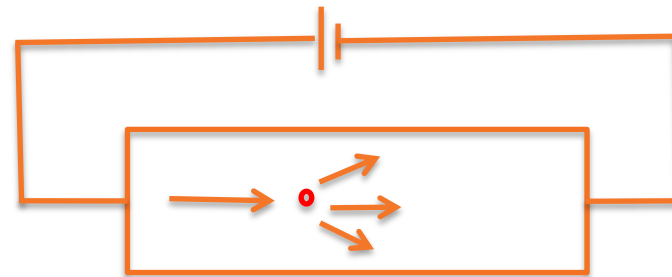
1/f noise

Superposition of simple processes with Lorentzian spectra having a broad distribution of time constants: e.g. carrier number fluctuations



[McWorther,
Proc. Conf. Ser
Phys,1957]

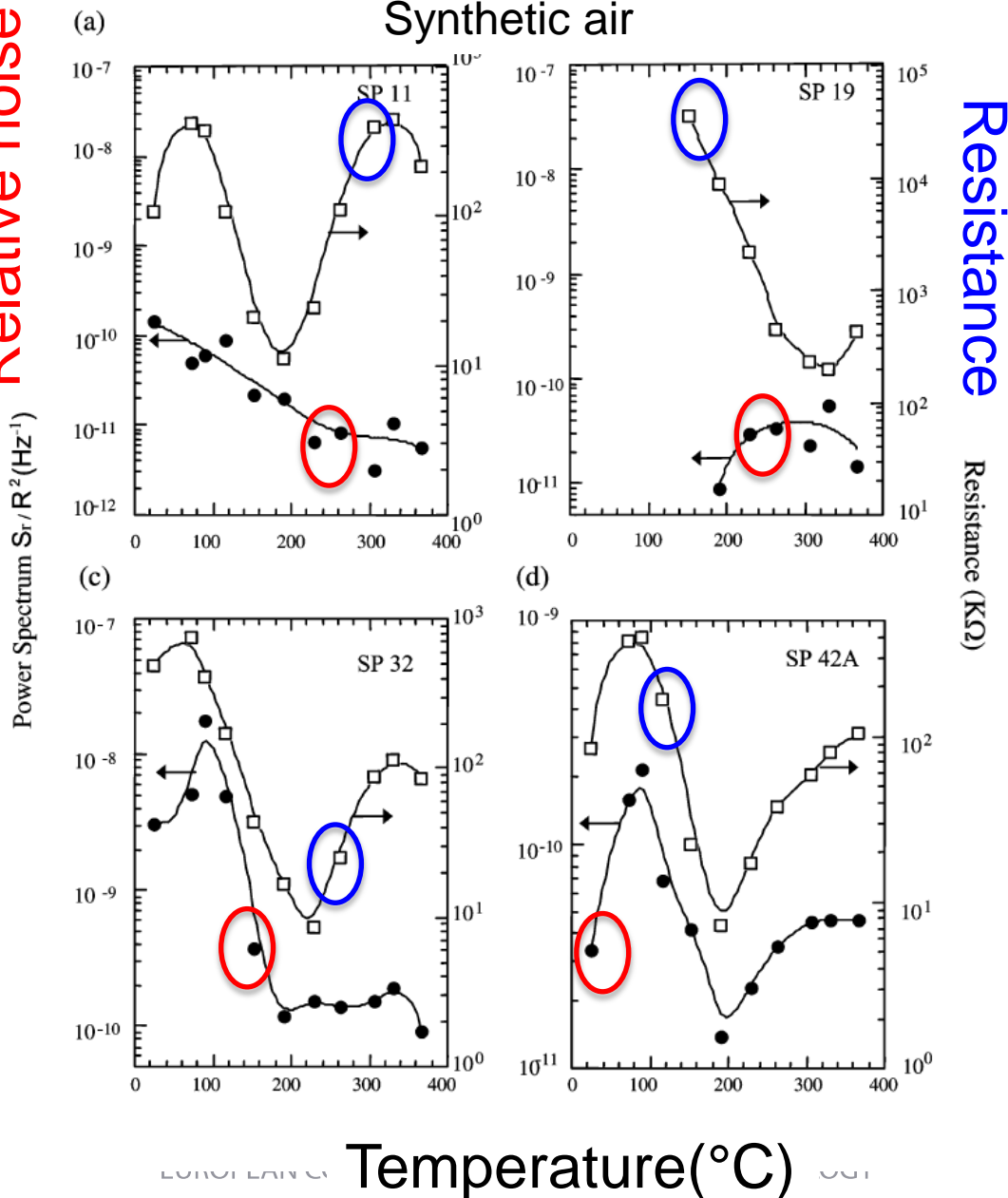
Complex scattering processes on defects and phonons: even a single scattering center can produce broadly distributed time constants



[Vandamme, Hooge I3E,
TED 55(2008)3070]

1/f noise in gas sensor: correlation $S_R/R^2(T)$ vs.

Relative noise



- Different Taguchi sensors (multigrain resistors)
 - Temperature as control parameter
 - power spectrum is not always correlated with changes in resistance
- [Solis& I3E Sens. J., 5(2005)1338]

→ 1/f noise can be used for sensing too

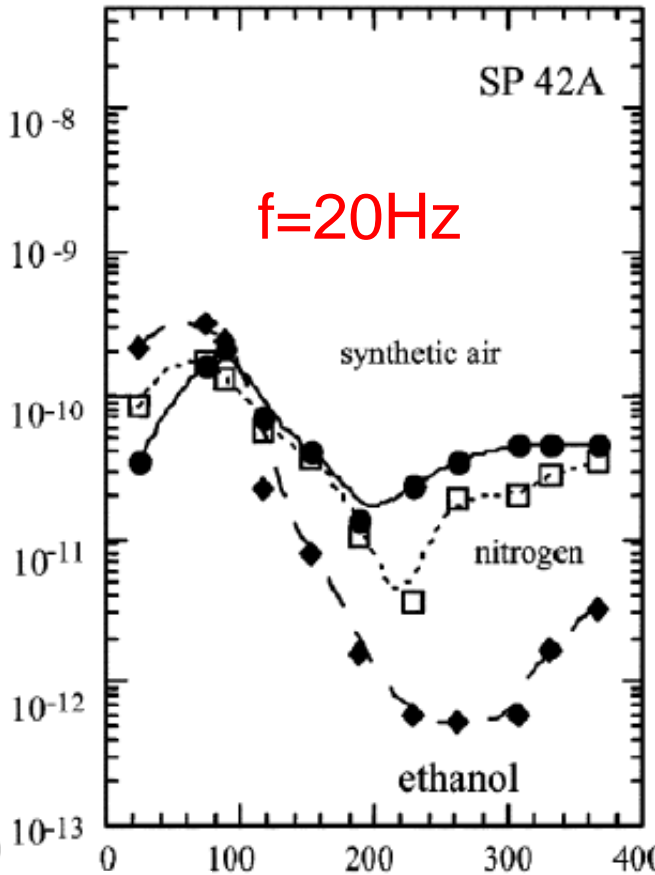
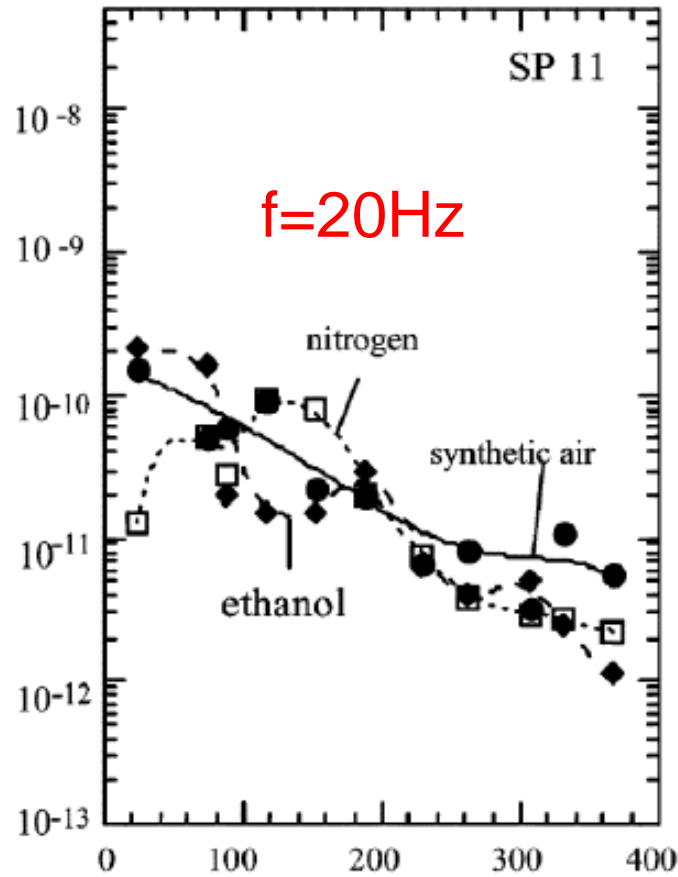
$$\frac{S_R(T)}{R^2(T)} \approx R^m$$

1/f noise: selectivity of $S_R/R^2(T)$ vs. gas

No selectivity of ethanol

Good selectivity of ethanol

Relative noise

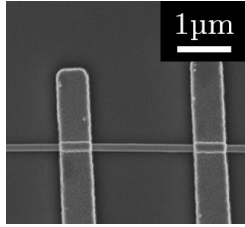


[Solis & I3E Sens. J.,
5(2005)1338]

Taguchi sensor

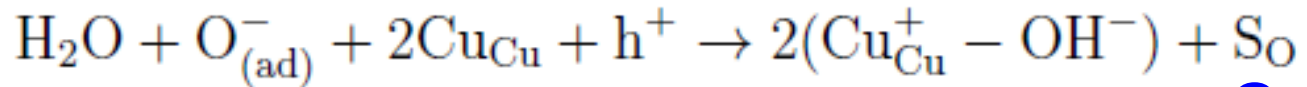
- temperature dependence of 1/f noise magnitude can give an information on selectivity in some sensors
- Additional info to $R(T)$

Effect of humidity on 1/f noise in CuO NW

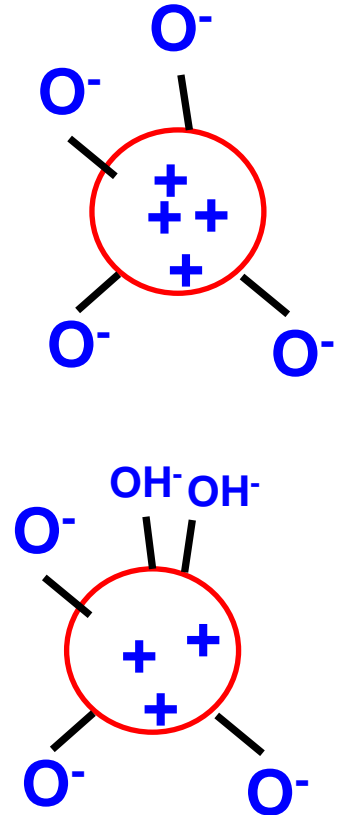
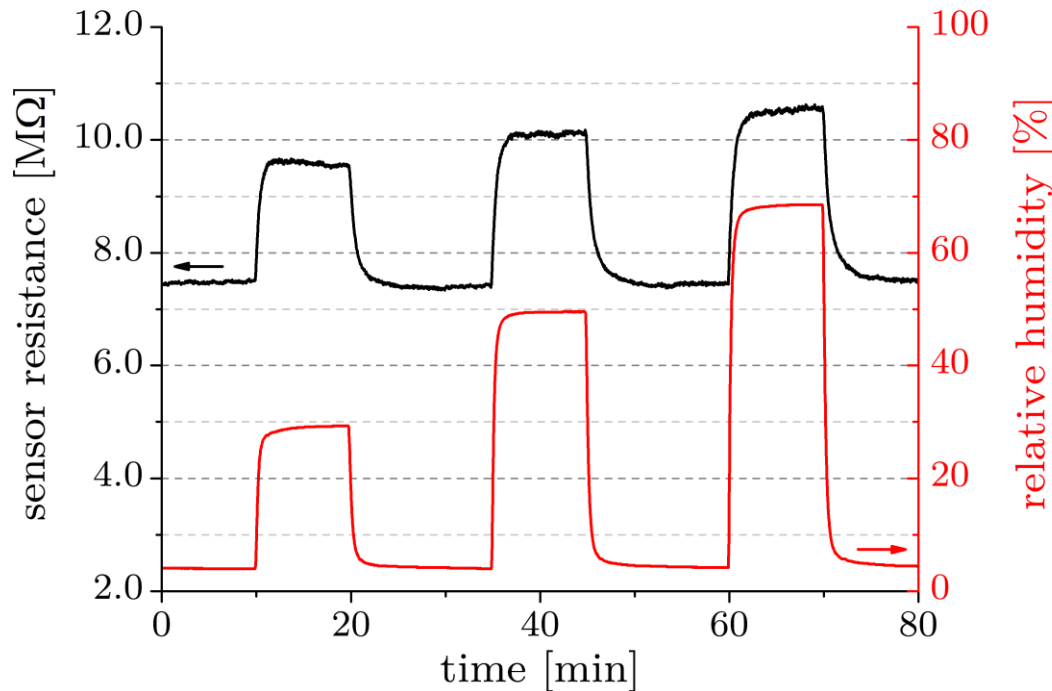


T=350°C, two-point configuration
Relative humidity 0→50% (RH50)

[Steinhauer&, APL,
107(2015)122112]



Single crystals NW: p-type conductivity

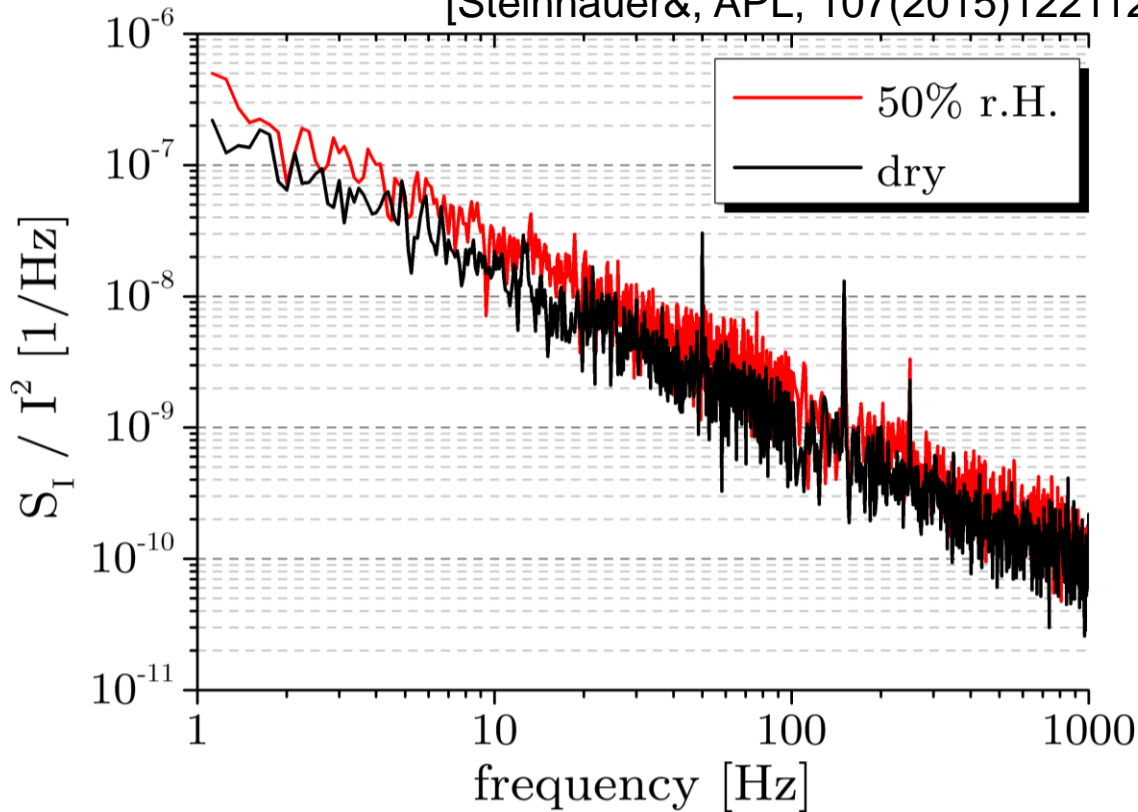


Water adsorption

- Humidity increases the resistance due to “compensation” of the negative surface charge by the hydroxyl group [M.Huebner& Sens. Act. B 153(2011)347-53]

1/f noise in CuO NW: effect of humidity

[Steinhauer&, APL, 107(2015)122112]



$$S_I = \frac{S_I(1\text{Hz})}{f^a}$$

Here:
 $a \cong 0.9-1.2$



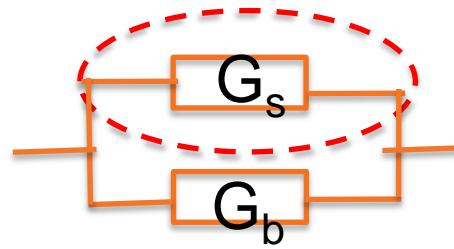
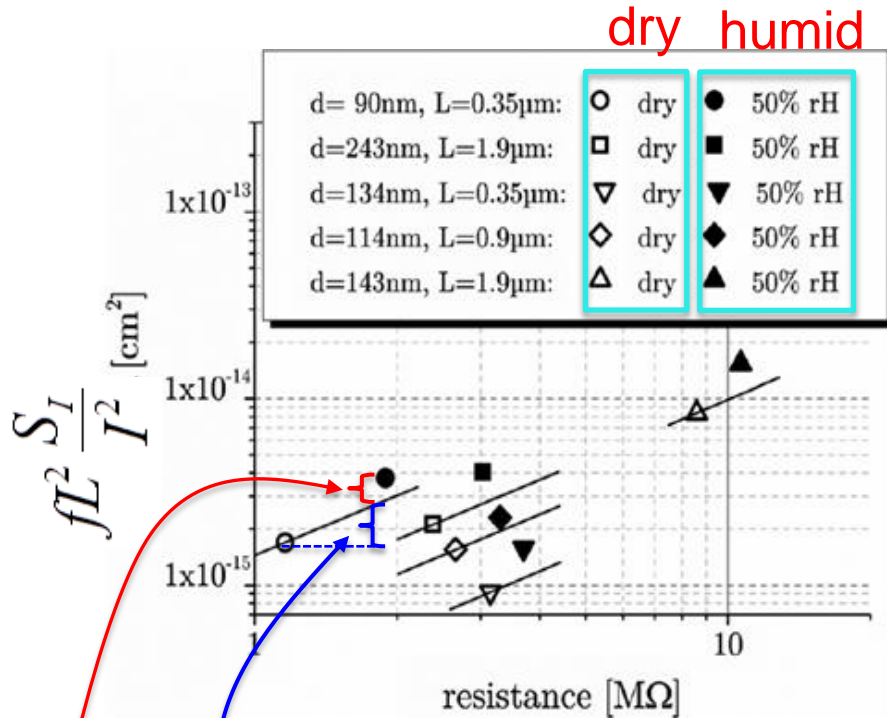
$$\frac{S_I}{I^2} = \frac{S_R}{R^2} = \frac{S_G}{G^2} = \frac{\alpha}{fN} = \frac{\alpha q \mu}{fL^2} R$$

α -Hooge's noise coeff.
 N-carrier number
 μ -carrier mobility
 q-element. charge
 L - NW length

- 1/f noise found (no Lorentzians)
- Humidity increases the relative noise
- We consider **mobility fluctuation model**

1/f noise in CuO NW: effect of humidity

NWs of different dimensions



Core/shell model
s-surface
b-bulk

Only surface resistance and surface noise changes due to gas are considered!!!

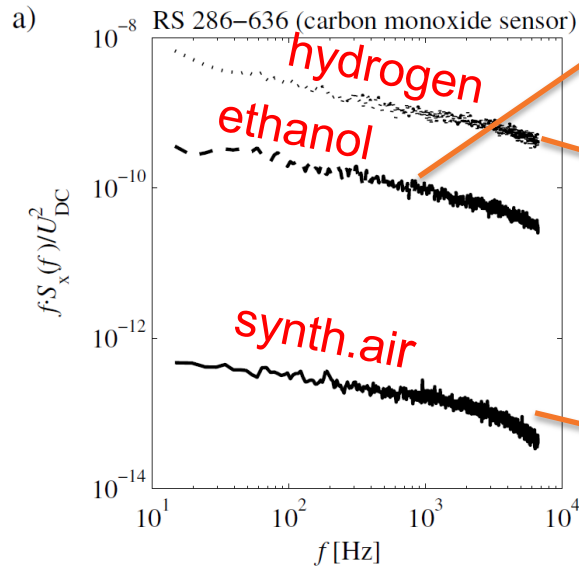
$$\frac{S_R}{R_{TOT}^2} = \frac{S_{G_s} + S_{G_b}}{G_{TOT}^2} = \frac{\frac{\alpha_s}{N_s f} G_s^2 + \frac{\alpha_b}{N_b f} G_b^2}{(G_s + G_b)^2} = \frac{K_s G_s + K_b G_b}{fL^2 (G_s + G_b)^2},$$

We consider fluctuations in scattering on surface potential roughness due to randomly distributed hydroxyl groups on NW surface

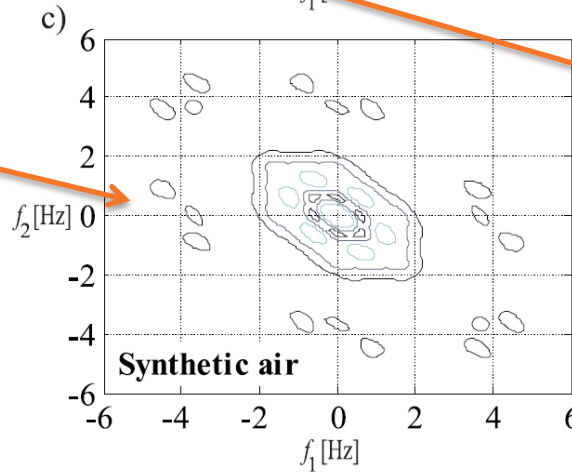
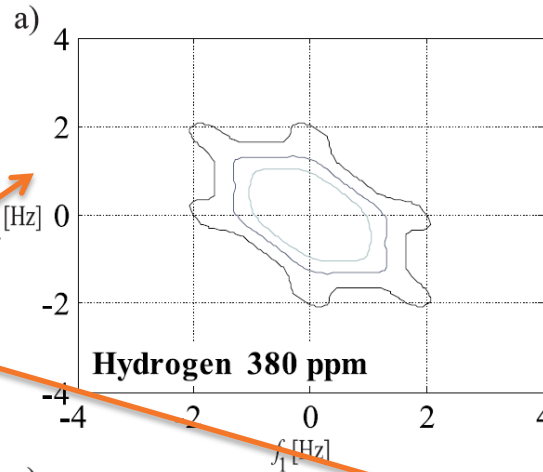
Change due to rise in surface noise

Higher order statistics-bispectrum

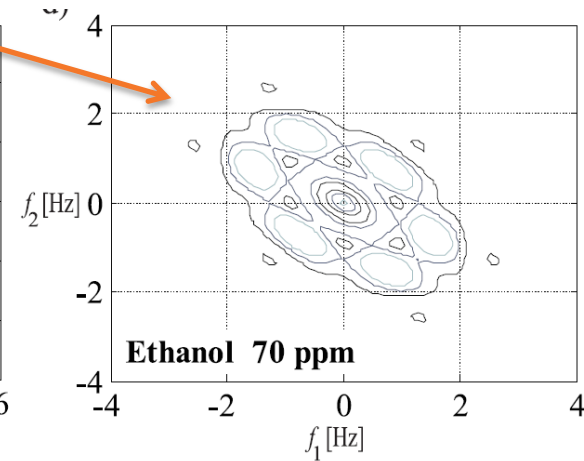
Power spectrum



[Smulko&, Sensors and Materials 16(2004)291]



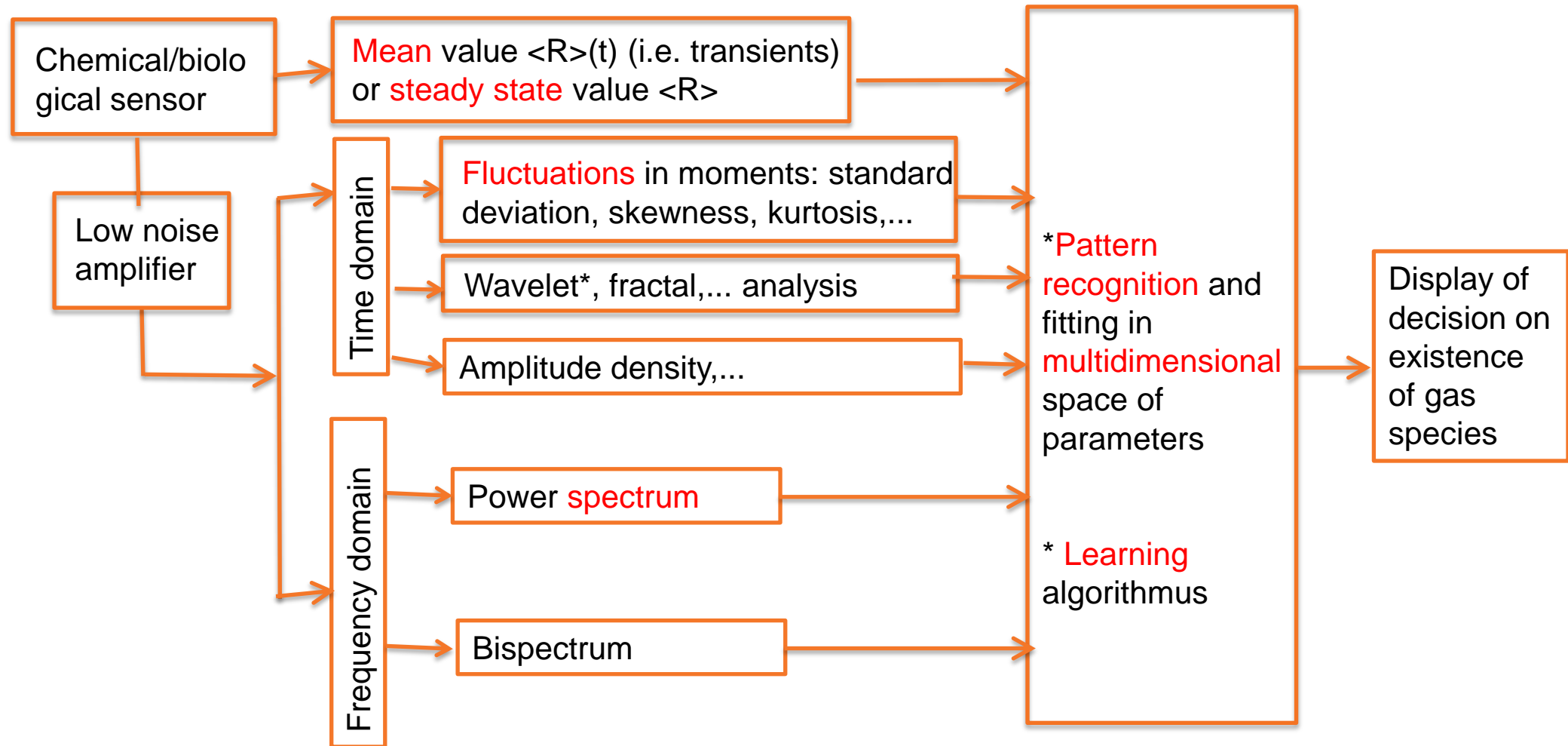
Contour plots of **bispectra** in Taguchi sensor designed for CO sensing



- special **fingerprints** of different gases in bispectra

$$S_{3x}(f_1, f_2) = \gamma_{3u} H(f_1) H(f_2) H^*(f_1 + f_2)$$

FES concept summary



Based on [Kwan & I3E Sens. J., 8(2008)706]: simplified + extended/updated

*Tulzer &, Nanotechnology 24(2013)315501

Precautions: What do we really measure?

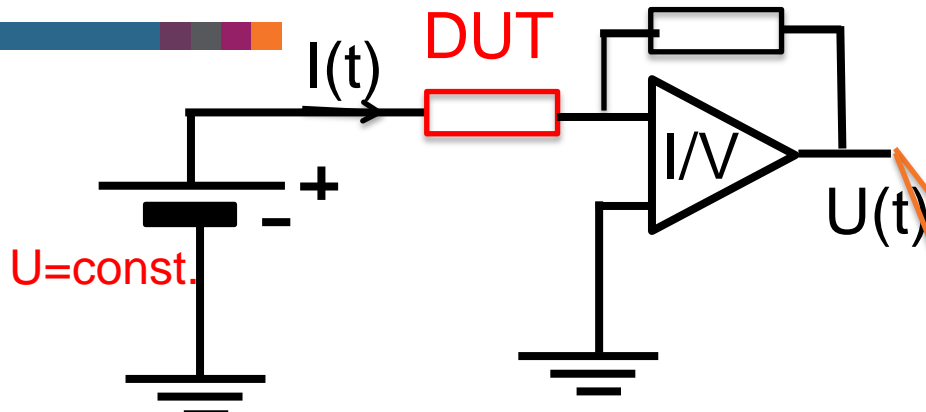
- **Defined measurement conditions:**
 - surface degassing prior to measurements
 - besides measurement of frequency spectra, recording/analysis of time domain waveforms is strongly suggested
 - Not to misinterpret e.g. contact RTS noise as A/D noise
 - Stationarity: Drifts \rightarrow $1/f^2$ dependence
 - \rightarrow Air and temperature fluctuations in measurement chamber and at the DUT should be low (laminar flow), [$dT(t) \rightarrow dR(t)$]
- **Spectral responses** of different gases in a mixture are **often not additive** (training algorithm necessary) [Solis & I3E Sens.J., 5(2005), 1338]
- Be careful in **interpretations**: even the noise mechanisms in “standard” electronic elements like resistors, FET, BJT, ... are still in discussion \rightarrow effects on sensor **optimization strategy**

Conclusions

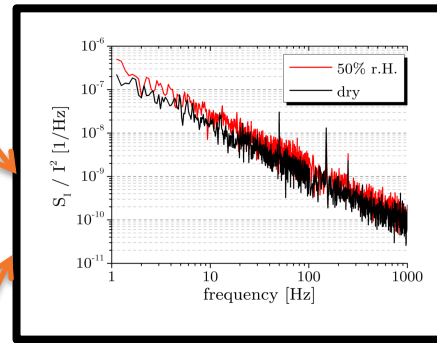
- Lorentzian-like and $1/f$ spectra can be used for gas sensing → additional information to $\langle R \rangle$ or $\langle R \rangle(t)$
- Pure adsorption – desorption noise is not yet experimentally demonstrated in frequency domain
- **Noise mechanisms in gas sensors are far from being understood!**
- Precautions on measurements conditions

Noise measurements

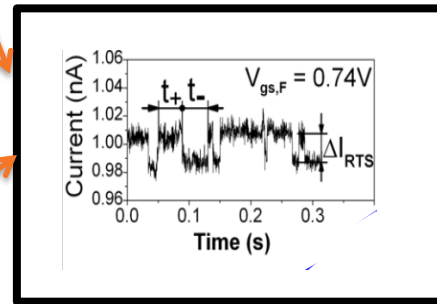
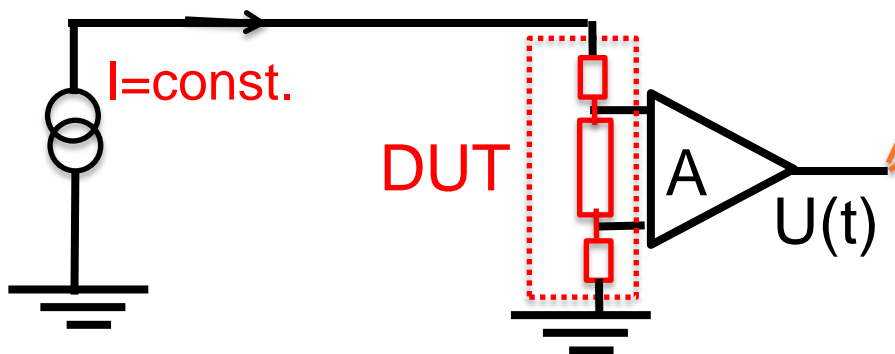
← **Two point** (contact noise and resistance included)



$$\frac{S_I}{I^2} = \frac{S_U}{U^2} = \frac{S_R}{R^2} = \frac{S_G}{G^2}$$



Spectrum analyzer:
Freq. domain



Digital oscilloscope:
Time domain

← **Four points** (contact noise and contact resistance not measured)

Supplement to 1/f noise in CuO NWs

$$\frac{S_R}{R^2} = \frac{S_{G_s} + S_{G_b}}{G^2} = \frac{\frac{\alpha_s}{N_s f} G_s^2 + \frac{\alpha_b}{N_b f} G_b^2}{(G_s + G_b)^2} = \frac{K_s G_s + K_b G_b}{f L^2 (G_s + G_b)^2},$$

$$\frac{K_b G_b + K_s G_s}{(G_b + G_s)^2} = \frac{K_b}{(G_b + G_s)} + \frac{G_s (K_s - K_b)}{(G_b + G_s)^2} = K_b R_{TOT} + G_s (K_s - K_b) R_{TOT}^2$$

$$\frac{1}{N_{s(b)}} = \frac{q \mu_{s(b)} R_{s(b)}}{L^2}$$

$N_{s(b)}$: number of carriers in the surface (bulk) regions of NW

μ -mobilities

$K_{s(b)}$ -coefficients

f -frequency

$G_{s(b)}$ -surface (bulk)

component of the conductance

$R_{TOT}=1/G_{TOT}$ -total resistance

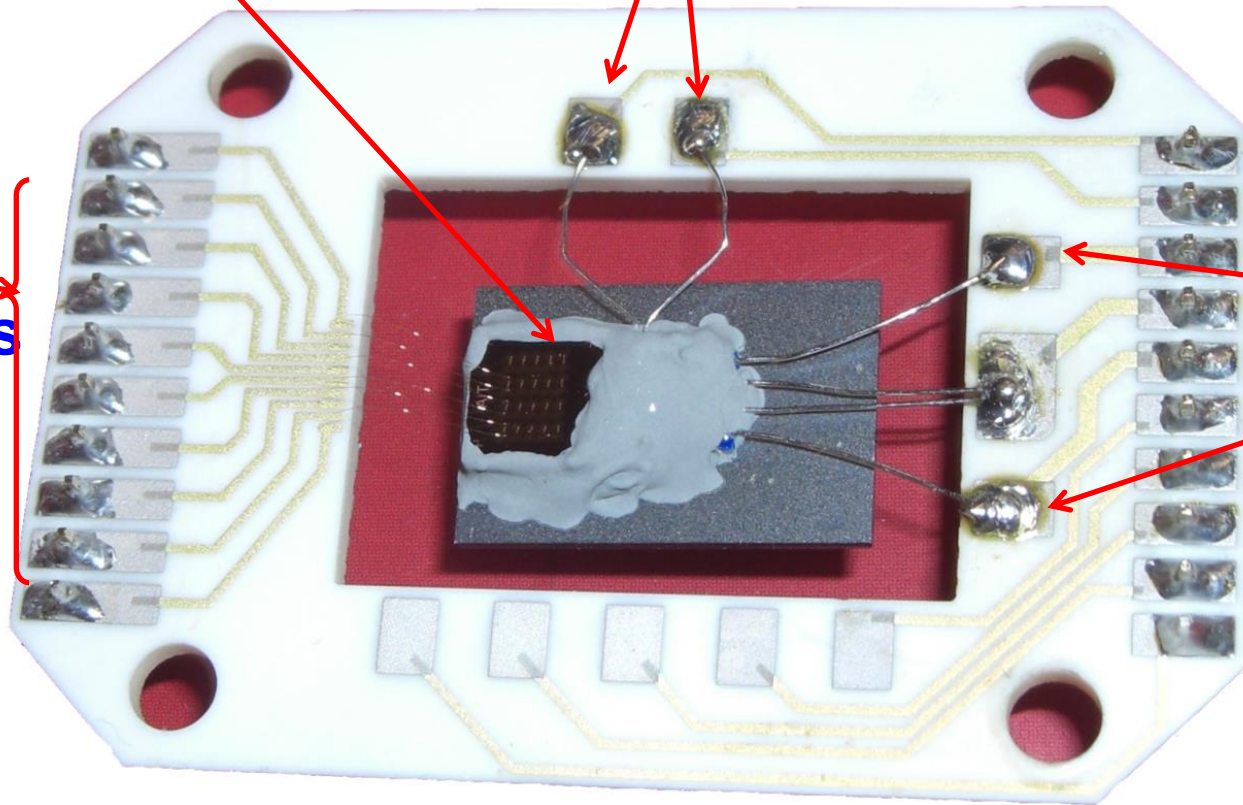
Test system

Chip with NWs

PT100 thermocouple

Bonded nanowires

Resistive heater element



- Temperatures up to 350°C
- Gas cell with controlled gas flow

Skewness and kurtosis

Let us suppose that the $x(t)$ sensor signal is sampled and recorded as a time series $x(n)$.

Simple measures of deviations¹⁰ from Gaussian distribution are skewness, γ_3 , and kurtosis, γ_4 .

These parameters are computed for a discrete-time random process $x(n)$ having standard deviation σ_x by the following relations:

$$\gamma_3 = \frac{1}{\sigma_x^3} E\left[\left(x(n) - E[x(n)]\right)^3\right] \quad (2)$$

$$\gamma_4 = \frac{1}{\sigma_x^4} E\left[\left(x(n) - E[x(n)]\right)^4\right] - 3 \quad (3)$$

Skewness: asymmetry

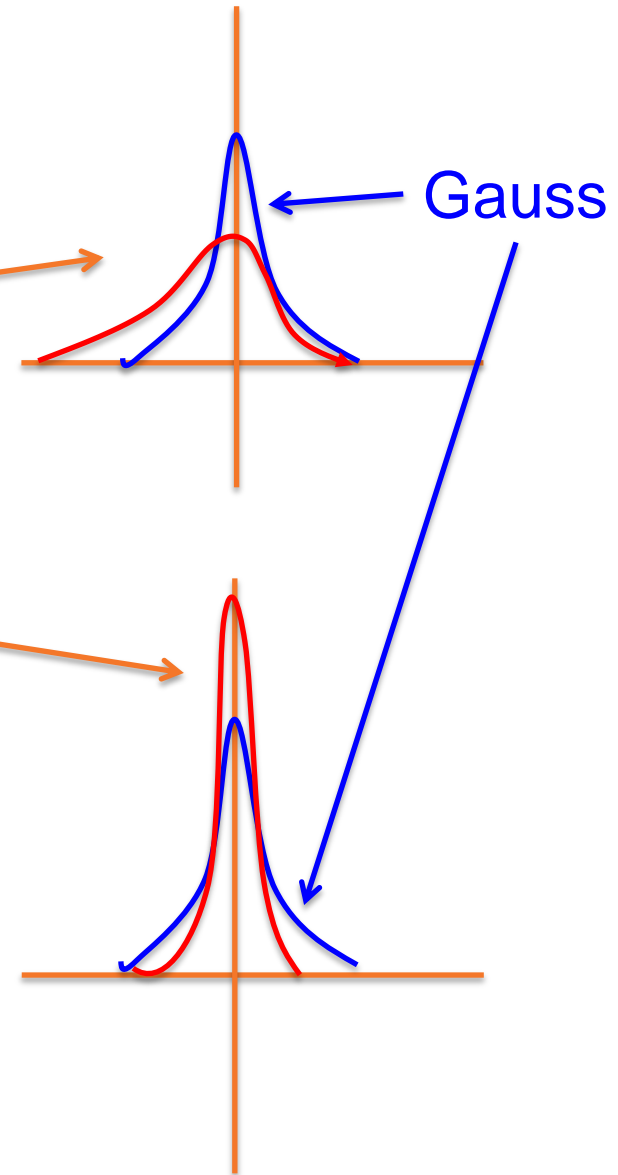
Kurtosis: peakness

where $E[\cdot]$ denotes an average. The skewness describes the degree of symmetry and the kurtosis

Differences in respect to Gaussian
amplitude distribution

[Smulko&, Sensors and
Materials 16(2004)291]

measures the relative peakedness of the distribution. Both measures are equal to zero for a Gaussian process.



Bispectrum

- axial symmetry of spectra → stationary process
- magnitude is near zero → the non zero values is due to a weak non-Gaussian component in the amplitude distribution]

An important tool to investigate the non-Gaussian component of the stochastic sensor signal is the bispectrum¹⁰⁻¹¹. The bispectrum function is the second-order Fourier transform of the third-order cumulant¹¹:

$$S_{3x}(f_1, f_2) = \sum_{k=-\infty}^{\infty} \sum_{l=-\infty}^{\infty} C_{3x}(k, l) e^{-j2\pi f_1 k} e^{-j2\pi f_2 l} \quad (4)$$

where $C_{3x}(k, l) = E[x(n)x(n+k)x(n+l)]$ is the third-order cumulant of the zero-mean process $x(n)$. The bispectrum is a two-dimensional complex function. Usually, its absolute value is analyzed, which is a three-dimensional landscape. The bispectrum function is equal to zero for processes with zero skewness, i.e. for Gaussian processes. The bispectrum of two statistically independent random processes equals the sum of the bispectra of the individual random processes. It is an important property of bispectra that Gaussian components in the recorded stochastic process are eliminated and only the non-Gaussian component are seen¹¹.

[Smulko&, Sensors and Materials 16(2004)291]

[Kwan& I3E
Sens.J.,8(2008)706]

$$S_{2x}(f) = \gamma_{2u} |H(f)|^2 \quad (8)$$

$$S_{3x}(f_1, f_2) = \gamma_{3u} H(f_1)H(f_2)H^*(f_1 + f_2) \quad (9)$$

where $H(f)$ is the frequency response. It can be seen from (8) and (9) that the power spectrum does not carry any information about the phase of $H(f)$, while if $u(n)$ is non-Gaussian, the phase information can be recovered with the bispectrum.